

Lesson 2.3: Order of Operations with Powers

1. Evaluate.

a) $5^2 + 3$

b) $5^2 - 3$

c) $5 + 3^2$

d) $5 - 3^2$

e) $(5 + 3)^2$

f) $(5 - 3)^2$

g) $5^2 + 3^2$

h) $5^2 - 3^2$

2. Evaluate.

a) $4^3 \times 2$

b) $4^3 \div 2$

c) 4×2^3

d) $4 \div 2^3$

e) $(4 \times 2)^3$

f) $(4 \div 2)^3$

g) $4^3 \times 2^3$

h) $4^3 \div 2^3$

3. Evaluate.

a) $(18 \div 3^2 + 1)^4 - 4^2$

b) $3^3 \div 9(3^0 - 2^2)$

c) $(12^2 + 5^3)^0 - 2[(-3)^3]$

d) $(7 - 5)^3 \times (8 + 2)^4$

e) $(4^2 \times 1^5)^2$

f) $[(-3)^4 - (-2)^3]^0 \div [(-4)^3 - (-3)^2]^0$

4. Insert brackets to make each statement true.

a) $15 \div 3 + 2 \times 4^2 - 5 = 43$

b) $15 \div 3 + 2 \times 4^2 - 5 = 27$

c) $15 \div 3 + 2 \times 4^2 - 5 = 107$

d) $15 \div 3 + 2 \times 4^2 - 5 = 64$

5. The formula for the volume, V , of a cylinder with height, h , and radius, r , is $V = \pi r^2 h$. Janet made 3 L of salsa and stores it in jars with a radius of 4 cm and a height of 10 cm.

She uses this expression to determine the number of jars she will need: $\frac{3000}{\pi \text{ () } \times 10}$

About how many jars will Janet need for the salsa?

6. Aftab, Shane, and Kyra got different answers when they evaluated this expression: $(-4)^2 - 3[(-9) \div 3]^2$ Aftab's answer was 97, Shane's answer was 43, and Kyra's answer was 19.

a) Show the correct solution.

b) **Show and explain how the students who got the wrong answer may have evaluated.**

Where did each student go wrong?

ANSWER KEY for Lesson 2.3

1. a) 28 b) 22 c) 14
d) -4 e) 64 f) 4
g) 34 h) 16

2. a) 128 b) 32 c) 32 d) $\frac{1}{2}$
e) 512 f) 8 g) 512 h) 8

3. a) 65 b) -9 c) 55
d) 80 000 e) 256 f) 1

4. a) $15 \div (3 + 2) \times 4^2 - 5 = 43$
b) $15 \div 3 + 2 \times (4^2 - 5) = 27$
c) $(15 \div 3 + 2) \times 4^2 - 5 = 107$
d) $15 \div 3 + (2 \times 4)^2 - 5 = 64$

5. About 6 jars

6. a) The correct solution:

$$\begin{aligned} (-4)^2 - 3[(-9) \div 3]^2 &= (-4)^2 - 3(-3)^2 = 16 \\ -3(9) &= 16 - 27 = -11 \end{aligned}$$

- b) Shane probably thought that $(-3)^2 = -9$; here is a possible incorrect solution:

$$\begin{aligned} (-4)^2 - 3[(-9) \div 3]^2 &= (-4)^2 - 3(-3)^2 = 16 \\ -3(-9) &= 16 + 27 = 43 \end{aligned}$$

Aftab probably multiplied -3 and -9 before evaluating in the brackets and applying the exponent. Here is a possible incorrect solution:

$$\begin{aligned} (-4)^2 - 3[(-9) \div 3]^2 &= 16 + (27 \div 3)^2 = \\ 16 + 9^2 &= 16 + 81 = 97 \end{aligned}$$

Kyra probably squared the 3 before doing any other operation. Here is a possible incorrect solution:

$$\begin{aligned} (-4)^2 - 3[(-9) \div 3]^2 &= 16 - 3[(-9) \div 9] \\ &= 16 - 3(-1) = 16 + 3 = 19 \end{aligned}$$